

# Dark Matter Accretion into Supermassive Black Holes

Sébastien Peirani

*Institut d'Astrophysique de Paris, 98 bis Bd Arago, 75014 Paris,  
France - Unité mixte de recherche 7095 CNRS - Université Pierre et Marie Curie\**

J.A. de Freitas Pacheco

*Observatoire de la Côte d'Azur  
Laboratoire Cassiopée - BP 4229 - 06304 - Nice Cedex 4 - France†  
(Dated: February 15, 2008)*

The relativistic accretion rate of dark matter by a black hole is revisited. Under the assumption that the phase space density indicator,  $Q = \rho_\infty/\sigma_\infty^3$ , remains constant during the inflow, the derived accretion rate can be higher up to five orders of magnitude than the classical accretion formula, valid for non-relativistic and non-interacting particles, when typical dark halo conditions are considered. For these typical conditions, the critical point of the flow is located at distances of about 30-150 times the horizon radius. Application of our results to black hole seeds hosted by halos issued from cosmological simulations indicate that dark matter contributes to no more than  $\sim 10\%$  of the total accreted mass, confirming that the bolometric quasar luminosity is related to the baryonic accretion history of the black hole.

PACS numbers: 04.70.Bw; 98.80.Cq

## I. INTRODUCTION

The presence of supermassive black holes (SMBHs) in the center either of elliptical galaxies or bulges of spiral galaxies seems presently to be a well established fact [1]. However, in spite of a large number of studies performed in the past years, the origin and evolution of these objects remain quite uncertain. Since SMBHs cannot be formed as a consequence of the evolution of stars having comparable mass, they are generally supposed to evolve from “seeds”, which grow by accretion inside the host galaxy. Moreover, the observation of quasars already at  $z \sim 6.5$ , when the universe was only  $\sim 0.85$  Gyr old, implies that the process of growth (accretion) must have been quite efficient at those early times.

Seeds could be intermediate mass ( $10^3$ - $10^4 M_\odot$ ) black holes formed in the collapse of primordial gas clouds [2, 3, 4] or in the core collapse of relativistic star clusters formed in starbursts, which may have occurred in the early evolution of galaxies [5]. Another appealing possibility is the formation of black hole seeds with masses in the range  $100$ - $300 M_\odot$ , resulting from the evolution of primordial massive stars [6]. These stars would have been formed at  $z \sim 15$ - $20$  in the high density peaks of the primordial fluctuation spectrum and their high masses would be a consequence of a very inefficient gas cooling at zero metallicity [7]. Besides forming black hole seeds, these massive stars could also have been the source of UV photons, responsible for the reionization of the universe.

The analysis of the bolometric quasar luminosity function at different redshifts indicates that most of the ac-

creted mass by black holes should be baryonic in origin [8, 9, 10]. Although expected to be small, the contribution of dark matter to the black hole growth is still uncertain. Unlike baryons, the infall of dark matter into black holes does not produce electromagnetic radiation and thus, does not contribute to the quasar luminosity, although some energetic photons could be produced either by annihilation or decay, if dark matter is constituted by neutralinos or sterile neutrinos respectively. Moreover, dark matter particles constitute a collisionless fluid and, consequently, the accretion process should be less efficient than that expected for a dissipative fluid. Even so, different scenarios were envisaged in which dark matter could give a significant contribution to the mass accretion budget. If halos embedding galaxies are constituted by self-interacting dark matter [11], then black holes with masses  $\geq 10^6 M_\odot$  could be formed directly as a consequence of relativistic core collapse of halos, following the gravothermal catastrophe [12]. In this scenario, no baryons and no prior star formation are required to form the massive black holes, but the high interaction cross-section necessary for the mechanism to work remains a difficulty. A different approach was considered in [13], where the dark matter accretion process was investigated in a scenario in which stars are already formed in the core of the galaxy. Dark matter particles scatter on stars in the vicinity of the central black hole, producing an important inflow as a consequence of diffusion in phase space and a mass growth scaling as  $M_{bh} \propto t^{9/16}$ . A similar mechanism was examined in [14] but, in this case, dark matter particles are scattered by molecular clouds. According to the authors, this process can boost the growth of the mass of seeds from about  $\sim 5 M_\odot$  up to  $\sim 10^4 M_\odot$ , which then grow by Eddington limited baryonic accretion. The growth of seeds under adiabatic conditions was considered by [15], who obtained

\*Electronic address: peirani@iap.fr

†Electronic address: pacheco@obs-nice.fr

a mass-age relation only in the isothermal case but with the resulting mass-velocity dispersion relation differing from observations. However, they have obtained a better agreement with data by assuming that black holes grow proportionally to the host halo mass.

In the present work, a new investigation on the dark matter accretion process into black holes is reported. Our approach gives an accretion rate significantly higher than that based on the well-known cross-section for capture by a black hole of non-relativistic and non-interacting particles. We have performed some numerical applications of our formula to the growth of seeds inside dark matter halos issued from cosmological simulations. These numerical calculations indicate that, if there is a coeval growth of seeds and their host halos, then dark matter contributes to no more than  $\sim 10\%$  of the total accreted matter, giving a further support to the usual assumption that the bolometric quasar luminosity function is related to the baryonic accretion history of SMBHs. This paper is organized as follows: in Section II, the equations describing the accretion process are presented; in Section III, numerical examples are discussed and finally, in Section IV, our main conclusions are given.

## II. THE ACCRETION MODEL

The relativistic steady spherical flow of a perfect gas into a black hole was first investigated by [16] and later by [17, 18, 19, 20] among others. Radiation transfer effects were considered in the pioneering work by Thorne and collaborators ([21, 22]) and more recently in [23, 24]. A comprehensive review on the subject can be found in [25]. It is worth mentioning that if the fluid has a non-zero angular momentum with respect to the black hole, then the spherical symmetry is broken. In this case, the accretion process is more complex since mechanisms of angular momentum transfer must be considered. Studies by [26] based on a “shell” accretion model indicate that the black hole growth factor is reduced if the fluid has a non-zero angular momentum. As we shall see later, our cosmological simulations do not have enough resolution to describe adequately the central region including the black hole influence radius. Thus, in the present investigation, we restrict our analysis to the spherical case.

Past investigations have shown that for an adiabatic flow of a gas with  $\gamma < 5/3$ , the only critical point of the flow which lies outside the horizon is the one corresponding to the Bondi solution. As we shall see below, a similar situation occurs in the case of a collisionless fluid. In our scenario, seeds appear around  $z \sim 12 - 15$  as a result of the core-collapse of massive stars [6] and are located in the center of dark matter halos. Near the central black hole of mass  $M_{bh}$ , we assume that the spacetime is described by the Schwarzschild metric and that a steady spherical inflow is set up inside the influence radius of the black hole, defined by  $r_* = 2GM_{bh}/\sigma_\infty^2$ , where  $\sigma_\infty$  is the velocity dispersion of dark matter particles of mass

$m$  in the core of the halo.

Under these conditions, the equations of motion are: the conservation of the mass flux

$$J_{;k}^k = 0 \quad (1)$$

and the energy-momentum flux conservation

$$T_{i;k}^k = 0 \quad (2)$$

where  $J^k = mn u^k$  is the mass-current density and the energy-momentum tensor is that of an ideal fluid, i.e.,  $T_i^k = (P + \varepsilon)u^k u_i - P\delta_i^k$ , with  $P$ ,  $\varepsilon$ ,  $n$ , being respectively the proper pressure, the proper energy density and the proper number density of the dark matter fluid.  $u^i = dx^i/ds$  is the 4-vector velocity, whose non-null components are  $u \equiv u^1 = dr/ds$  and  $u^0 = dt/ds$ . As in [16], one obtains from these equations

$$\frac{(P + \varepsilon)}{n} \left(1 - \frac{r_g}{r} + u^2\right)^{1/2} = k_1 \quad (3)$$

where  $r_g = 2GM_{bh}/c^2$  is the gravitational radius and  $k_1$  is a constant. Deriving eq. 3 with respect to the radial coordinate  $r$  and using the mass conservation equation (eq. 1), one obtains a “wind” equation, i.e.,

$$\frac{dlg}{dlg} \frac{u}{r} [u^2 - V^2 F(r, u)] + \left[\frac{r_g}{2r} - 2V^2 F(r, u)\right] = 0 \quad (4)$$

where

$$F(r, u) = \left(1 - \frac{r_g}{r} + u^2\right) \quad (5)$$

and

$$V^2 = \frac{dlg}{dlg} \frac{(P + \varepsilon)}{n} - 1 \quad (6)$$

The critical point of the flow occurs where both bracketed factors in eq. 4 vanish simultaneously, namely,

$$u_c^2 = \frac{r_g}{4r_c} \quad (7)$$

and

$$V_c^2 = \frac{u_c^2}{(1 - 3u_c^2)} \quad (8)$$

After decoupling, dark matter particles constitute a weakly interacting fluid. In the matter era, at higher redshifts, the universe evolves closely to the Einstein-de Sitter model. In this case, the distribution function  $f(\vec{u}, t)$  of dark matter particles is a function of integrals of the characteristics of the Vlasov equation, i.e.,

$$f(\vec{u}, t) = f(a(t)\vec{u}) \quad (9)$$

where  $a(t) \propto t^{2/3}$  is the scale factor and  $\vec{u} = (\vec{v} - H\vec{r})$  is the peculiar velocity. The distribution function must also satisfy the normalization condition

$$\int f(\vec{u}, t) d^3\vec{u} = mn(t) = \rho(t) = \frac{1}{6\pi G t^2} \propto a^{-3}(t) \quad (10)$$

where the small contribution of baryons to the total matter density was neglected. Under these conditions, the velocity dispersion of the peculiar velocity satisfies

$$\sigma^2 = \frac{\int u^2 f(\vec{u}, t) d^3 \vec{u}}{\int f(\vec{u}, t) d^3 \vec{u}} \propto \frac{1}{a^2(t)} \quad (11)$$

and the quantity  $Q = \rho(t)/\sigma^2 >^{3/2}$ , an indicator of the phase space density, is conserved during the expansion of the universe.

High resolution simulations of galaxy-size dark matter halos by [29] indicate an increase of  $Q$  toward the center. Similar results were obtained by [30], who have derived a power-law variation, e.g.,  $Q \propto r^{-\beta}$  for cluster-size halos, with  $\beta$  quite close to the value found by [29], namely  $\beta \simeq 1.87$ . No adequate explanation exists presently for such a power-law profile, although [31] suggests that it could be a consequence of an isotropic distribution function produced in the halo core by processes of relaxation related to the radial orbit instability. In fact, [31, 32] assuming that the evolution of halos is self-similar, derived the conditions required for the density profile as well as the phase density indicator  $Q$  be described by power laws. A density profile with a slope  $dlg\rho/dlgr = -2$ , typical of self-similar radial infall, can be consistent with phase space profiles either of the form  $Q = \rho/\sigma^3$  or  $Q = \rho/\sigma^2$ . Here we adopt the usual definition, which is supported by the results of different cosmological simulations.

As structures begin to form as well as to accrete matter and merger together, rapid variations in the gravitational potential contribute to the relaxation of the system through “violent relaxation” ([27]). This process leads to a smooth mass-independent distribution function as a result of the gravitational scattering of particles. Violent relaxation produces a more mixed system in phase space, reducing the value of the coarse-grained distribution function or, in other words, reducing the value of  $Q$  ([28]). Therefore, as a consequence of such a mechanism, the velocity dispersion of dark matter particles, at late epochs, inside halos is not negligible as one would expect taking into account only the expansion of the universe (eq. 11). In this case, including the energy of the random peculiar motion, the total energy density can be written as

$$\varepsilon = mnc^2 + \frac{1}{2}mn\sigma^2 \quad (12)$$

and, consequently

$$(P + \varepsilon) = mnc^2 + \frac{5}{6}mn\sigma^2 \quad (13)$$

Notice that, as mentioned previously, the phase space density increases toward the center as  $Q \propto r^{-1.87}$ , but one expects a convergence to a finite value close to the black hole influence radius. Once the inflow develops, we hypothesize that the quantity  $Q$  remains constant. This assumption is reasonable if no important phase space mixing occurs during the inflow. According to cosmological simulations by [33, 34], the phase space indicator

$Q$  estimated in the core of halos evolves in two distinct phases. An early and fast phase in which the decrease of  $Q$  is associated to virialization just after the first shell crossing, following the gravitational collapse of the halo. In a second late and long phase, a slow decrease of  $Q$  is observed, consequence of continuous matter accretion and merger episodes. Since the infall time scale of dark matter particles onto the central black hole is small in comparison with the characteristic time scale in which the phase space indicator varies, namely,  $Q/|(dQ/dt)| \sim 0.7$  Gyr (typical value derived from the aforementioned simulations), we can suppose that the flow is steady but adjusted to the slowly varying conditions of the environment. In this case, eq. 13 can be recast as

$$(P + \varepsilon) = mnc^2 + \frac{5}{6}m\frac{n^{5/3}}{Q_n^{2/3}} \quad (14)$$

Notice that, in the above equation, we have defined  $Q_n = Q/m = n/\sigma^3$  and that the assumption of keeping  $Q$  constant during the inflow is similar to that of considering the compression of a perfect gas with  $\gamma = 5/3$ . In fact, since the entropy density satisfies  $s \propto -\log Q$ , the assumption that  $Q$  remains constant is equivalent to the hypothesis of an adiabatic inflow, although with a different adiabatic constant.

Using eq. 14, one obtains

$$\begin{aligned} \frac{d(P + \varepsilon)}{dn} &= mc^2 + \frac{25}{18}m\left(\frac{n}{Q_n}\right)^{2/3} \\ &= \frac{(P + \varepsilon)}{n} \left[1 + \frac{5}{9} \frac{mn^{5/3}Q_n^{-2/3}}{(P + \varepsilon)}\right] \end{aligned} \quad (15)$$

and replacing the equation above into eq. 6, one obtains

$$V^2 \simeq \frac{5}{9} \frac{n^{2/3}Q_n^{-2/3}}{c^2} - \frac{25}{54} \frac{n^{4/3}Q_n^{-4/3}}{c^4} \quad (16)$$

where a Taylor series up to the second order was used. The constant  $k_1$  in eq. 3 can be calculated by imposing that for  $r \gg r_g$  we have  $u \rightarrow 0$ . Thus, one obtains

$$k_1 = mc^2 + \frac{5}{6}m\left(\frac{n_\infty}{Q_n}\right)^{2/3} \quad (17)$$

where  $n_\infty$  stands for the dark matter particle number density far away from the black hole, where the flow velocity is negligible. At the critical point, eq. 3 can be rewritten as

$$\begin{aligned} [mc^2 + \frac{5}{6}m\left(\frac{n_c}{Q_n}\right)^{2/3}](1 - 3V_c^2)^{1/2} &= \\ &= mc^2 + \frac{5}{6}m\left(\frac{n_\infty}{Q_n}\right)^{2/3} \end{aligned} \quad (18)$$

where  $n_c$  is the number density at the critical point. Replacing eq. 16 into the equation above, one obtains after some algebra,

$$\frac{n_c}{n_\infty} \simeq \frac{6}{5} \left(\frac{c}{\sigma_\infty}\right)^2 \quad (19)$$

which permits to estimate the density at the critical point as a function of physical conditions of the halo, far away the black hole. Since the flow velocity at the critical point satisfies  $u_c^2 \ll 1/3$ , from eq. 8 and eq. 16 one obtains to the first order

$$u_c^2 \simeq \frac{5}{9} \frac{n_c^{2/3}}{Q^{2/3} c^2} \quad (20)$$

and, using the relation above for the density at the critical point and the fact that  $Q_n = n_\infty/\sigma_\infty^3$ , one obtains finally

$$u_c^2 \simeq 0.627 \left( \frac{\sigma_\infty}{c} \right)^{2/3} \quad (21)$$

Replacing this result into eq. 7, one obtains for the critical radius

$$r_c \simeq 0.398 \left( \frac{c}{\sigma_\infty} \right)^{2/3} r_g \simeq 0.398 \left( \frac{\sigma_\infty}{c} \right)^{4/3} r_* \quad (22)$$

For typical halos with  $\sigma_\infty$  in the range 50-300 km/s, the critical radius is located in the interval 130-40 times the horizon radius, well inside the influence sphere. It is interesting to recall that, for an ideal gas, the critical point is located at

$$r_c \simeq \frac{(5-3\gamma)}{8} \left( \frac{c}{a_\infty} \right)^2 \quad (23)$$

where  $a_\infty$  is the sound velocity far away from the black hole. This relation implies that the critical point is outside the horizon only if  $\gamma < 5/3$  (see [17]).

Once the parameters at the critical point are known, the accretion rate is given by

$$\begin{aligned} \frac{dM_{bh}}{dt} &= 4\pi r_c^2 \left( \frac{T_0^1}{c} \right) \\ &= \frac{27\pi}{4\sqrt{125}} r_g^2 c^4 Q = \frac{27\pi}{\sqrt{125}} (GM_{bh})^2 Q \end{aligned} \quad (24)$$

where only first order terms were retained. Notice that for non-relativistic and non-interacting particles, the expected accretion rate is [35]

$$\frac{dM_{bh}}{dt} = 4\pi r_g^2 \rho_\infty \frac{c^2}{v_\infty} \quad (25)$$

where  $v_\infty$  is the relative velocity of particles “at infinity” with respect to the black hole. This equation predicts an accretion rate smaller by a factor  $27c^2/(16\sqrt{125}\sigma_\infty^2)$  than eq. 24, which is of the order  $10^5$ , if estimated in the core of a typical dark halo.

### III. NUMERICAL APPLICATION

In this section, an application of the results obtained previously is performed. Firstly, we emphasize that we do not intend to present here a detailed model for the

growth of black holes located in the core of halos. This problem will be discussed in a future paper. Our purpose here is to give only a rough estimate of the dark matter fraction accreted by the black hole, assuming that our formula (eq. 24) gives a correct description of the inflow.

Halos investigated in this work were selected from catalogs prepared by [33], which were based on systems identified in cosmological N-body simulations, using an adaptive particle-particle/particle-mesh ( $AP^3M$ ) code ([36]). The adopted cosmological parameters were  $h = 0.65$ ,  $\Omega_m = 0.3$  and  $\Omega_\Lambda = 0.7$ , with the power spectrum normalization taken to be  $\sigma_8 = 0.9$ . Simulations were performed in a box of side  $30h^{-1} \text{ Mpc}$ , including  $256^3$  particles, corresponding to a mass resolution of  $2.05 \times 10^8 M_\odot$  and covering the redshift interval  $0 \leq z \leq 50$ . Halos were initially detected by using a friends-of-friends (FOF) algorithm ([37]) and, in a second step, unbound particles were removed by an iterative procedure. In the total, about 9000 gravitationally bound halos were detected at  $z = 0$ . For more details, see [33, 38]. However, the mass history in the redshift range  $0 \leq z \leq 10$  could be followed only for 35 halos with enough particles ( $N \geq 50$ ). The phase space density indicator  $Q$ , was calculated according to the prescription detailed in [33], inside a spherical volume whose radius is equal to one tenth of the gravitational radius of the halo, which is defined as the “core” region.

The present observations indicate that in all massive galaxies where the masses of bulges and central black holes have been estimated from kinematic data, there is a robust correlation between them [39, 40, 41]. Moreover, other investigations have shown conclusively that not only there is a link between the black hole mass and the bulge mass but also with the circular velocity [42]. If circular motions probe the halo potential, then a relation between the present black hole mass and the present halo mass is also expected. These relations suggest that black holes grew coevally with their host galaxies and associated halos [43]. Here, this assumption will be adopted and, consequently, the black hole growth rate is given by

$$\frac{1}{Y(t)} \frac{dY(t)}{dt} = \alpha \frac{d \ln M_H(t)}{dt} \quad (26)$$

where  $\alpha=1.27$  is a constant (see, eq. 28 below) and  $Y(t) = M_{bh}(t)/M_{bh}(0)$  is the black hole mass, measured in units of its present mass  $M_{bh}(0)$ . The right member of eq. 26 represents the mass growth rate of the host dark halo.

At any instant, the total mass of the black hole is the sum of the amount of accreted baryonic and dark matter masses. If  $X(t)$  is fraction of accreted dark matter at instant  $t$  then, using eq. 24 and the previous definitions, one obtains

$$\frac{dX(t)}{dt} = -\frac{X(t)}{Y(t)} \frac{dY(t)}{dt} + KY(t)Q(t) \quad (27)$$

where, as in eq. 26, the time is in units of  $H_0^{-1}$  and the constant  $K$  is equal to  $K = 27\pi G^2 M_{bh}(0)/\sqrt{125} H_0 =$

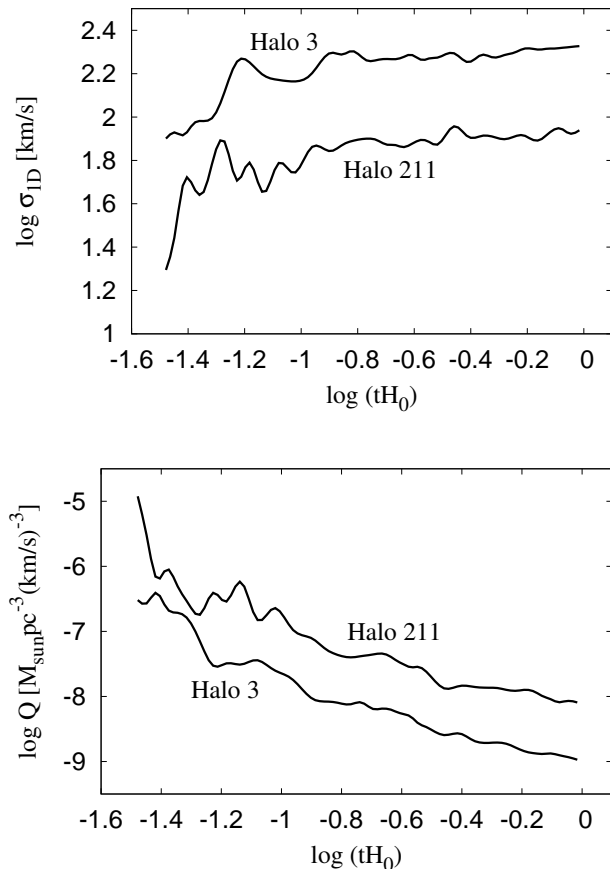


FIG. 1: Evolution of the velocity dispersion (km/s) inside the core of halos 3 and 211 (upper panel). Evolution of the phase density ( $M_{\odot} pc^{-3} km^{-3} s^3$ ) in core for the same halos (lower panel). Time is given in units of  $H_0^{-1}$ .

$2.143(M_{bh}(0)/M_{\odot})$ . The numerical value corresponds to the phase space density taken in units of  $M_{\odot} pc^{-3} km^{-3} s^3$ .

The calculation procedure was the following: for a given halo having presently a mass  $M_H$ , the black hole mass was estimated by the relation derived by [42], namely

$$M_{bh}(0) = 1.1 \times 10^7 \left( \frac{M_H}{10^{12} M_{\odot}} \right)^{1.27} M_{\odot} \quad (28)$$

and, consequently, the value of the constant  $K$  can be calculated. The system of differential eqs. 26 and 27 was then solved numerically, using the mass and phase space density derived from cosmological simulations. The initial values of  $Y$  and  $X$  were varied until the solution gives  $Y = 1$  for the present black hole mass.

For studied halos, with present masses in the range  $7.5 \times 10^{11} - 9.54 \times 10^{12} M_{\odot}$ , we have found that the fraction of dark matter accreted by the halo is in the range 1-10%.

In order to exemplify, in figure 1 it is shown the evolution of two halos whose final masses are respectively

$7.46 \times 10^{11} M_{\odot}$  (halo 211) and  $8.06 \times 10^{12} M_{\odot}$  (halo 3). The upper panel shows the evolution of the velocity dispersion whereas the lower panel shows the evolution of the phase space density indicator  $Q$ . Both quantities were calculated in the core region, as defined above. Notice that to make easier the comparison with observations, we have plotted the 1D-velocity dispersion and that the quantity  $Q$  was also calculated with respect to  $\sigma_{1D}$ . The 3D values can be obtained multiplying the 1D-velocity dispersion by  $\sqrt{3}$  and dividing  $Q_{1D}$  by  $\sqrt{27}$ . Notice also that the more massive halo (halo 3) has a higher velocity dispersion but a lower phase density  $Q$ , in agreement with the fact that the late quantity, for a given redshift, scales as  $Q \propto M^{-0.82}$  ([33]). The black hole mass evolution in the considered halos is shown in figure 2 (upper panel), where it is possible to see that the growth is not uniform, retracing the mass history of halos. Sudden increases in mass growth represent merger episodes. The fraction of accreted dark matter is shown in the lower panel of figure 2. At  $z \sim 10$ , the fraction of dark matter is about 0.005 for both halos whereas it attains a value around 0.02 for the less massive halo (halo 211) and about 0.05 for halo 3. Notice the fast increase in the dark matter contribution for  $z < 2$ , consequence of a decreasing merger rate after such a redshift. This affects the dark matter accretion in two aspects: firstly, decreasing the contribution of baryonic matter to the black hole growth and secondly, the decreasing merger rate implies also that  $Q$  decreases more slowly than the black hole growth rate and, consequently, the relative contribution of dark matter increases.

In figure 3 the baryonic and dark matter accretion rates are compared for both halos. Different peaks in the baryonic accretion rate are associated to minor or major merger episodes, with the maximum rate occurring around  $z \sim 1.5$ . Halo 3 is an example where for two short time intervals the accretion rate of dark matter became higher than the baryonic accretion rate. The baryonic accretion rate will be probably reduced by a factor of 2-6 if the star formation process is included, an aspect presently under investigation, based on detailed cosmological simulations.

#### IV. CONCLUSIONS

The accretion of dark matter into black holes located in the center of galaxies and their halos was studied. The accretion rate was derived by solving the equations for a relativistic steady spherical symmetric inflow, under the assumption that the phase space density indicator  $Q = \rho/\sigma^3$  remains constant. This hypothesis is equivalent to say that the inflow is adiabatic, since the entropy density satisfies  $s \propto -\log Q$ .

We found that our solution predicts that the critical radius is always outside the black hole horizon and that the flow radial velocity at the critical point is of the order of few percent of the speed of light. After the crossing the

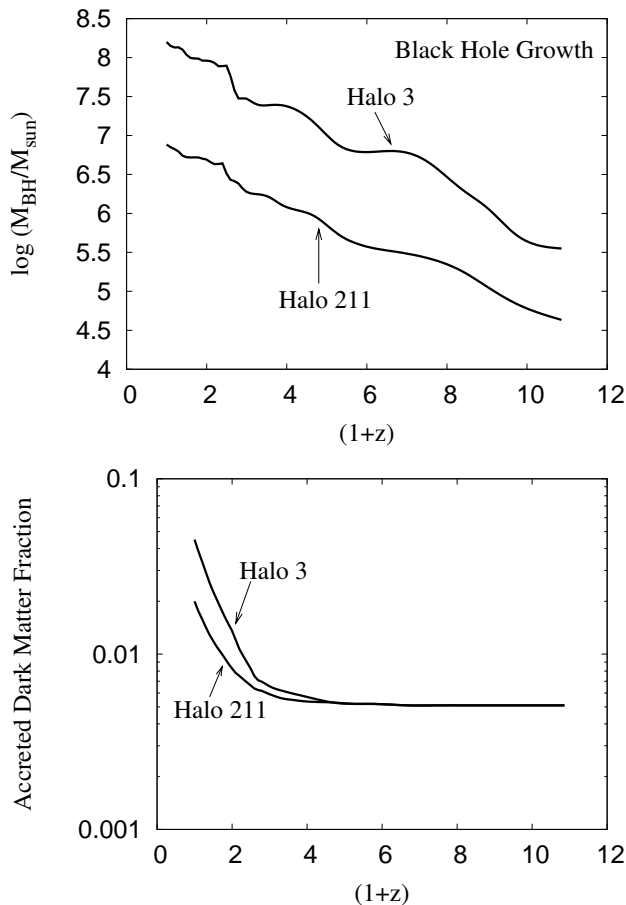


FIG. 2: In the upper panel it is shown the mass evolution of black holes while in the lower panel the evolution of the fraction of accreted dark matter is shown.

critical point, numerical solutions of equations describing the flow indicate that the velocity and the density have power-law profiles, e.g.,  $u \propto 1/r^{0.6}$  and  $\rho \propto 1/r^{1.4}$ , a behavior quite close to that resulting from the classical “free-fall” solution. Notice that the growth of black holes embedded in a collisionless fluid was also studied by considering that orbits shrink inside the influence sphere but conserving their adiabatic invariants [44]. In this case, a density “spike” with a profile  $\rho \propto 1/r^{1.5}$  results, similar again to our inflow model.

The derived accretion rate for a steady flow is proportional to the square of the black hole mass and to the dark matter phase space density indicator  $Q = \rho_\infty/\sigma_\infty^3$ . For black holes hosted by typical dark halos, the present

accretion rate is about five orders of magnitude higher than the usual rate derived by using the capture cross section for non-relativistic and non-interacting particles.

Numerical applications of the derived formula were made by computing the growth of black holes inside halos issued from cosmological simulations. We found that dark matter contributes to no more than 10% of the total mass accreted by black hole seeds. This result is consistent with the fact that the time integrated bolometric

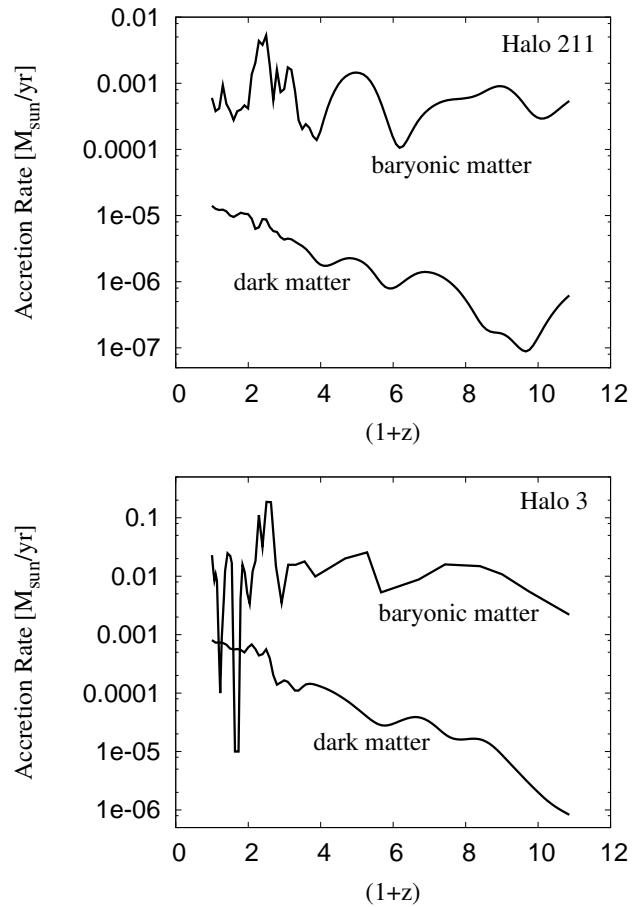


FIG. 3: Evolution of the baryonic and dark matter accretion rates for halo 211 (upper panel) and halo 3 (lower panel).

luminosity of quasars gives a present black hole mass density comparable with other independent estimates, indicating that most of the accreted mass by seeds is baryonic in origin.

- [1] J.Kormendy and K. Gebhardt, in Proceedings of the 20th Symposium of Relativistic Astrophysics, eds. H. Martel and J.C. Wheeler, p.363 (astro-ph/0505463)
- [2] M.G. Haehnelt and M.J. Rees, MNRAS 263, 168 (1993)
- [3] D.J. Eisenstein and A. Loeb, ApJ 443, 11, (1995)

- [4] S.M. Koushiappas, J.S. Bullock and A. Dekel, MNRAS 354, 292 (2004)
- [5] S.L. Shapiro, ApJ 613, 1213 (2004)
- [6] A. Heger, C.L. Fryer, S.E. Woosley, N. Langer and D.H. Hartmann, ApJ 591, 288 (2003)

- [7] B.J. Carr, J.R. Bond and W.D. Arnett, *ApJ* 277, 445 (1984)
- [8] A. Soltan, *MNRAS* 200, 115 (1982)
- [9] T.A. Small and R.D. Blanford, *MNRAS* 259, 725 (1992)
- [10] P.F. Hopkins, G.T. Richards and L. Hernquist, *ApJ* 654, 731 (2007)
- [11] R. Davé, D.N. Spergel, P.J. Steinhardt and D. Wandelt, *ApJ* 547, 574 (2001)
- [12] S. Balberg and S.L. Shapiro, *PRL* 88, 101301 (2002)
- [13] M.I. Zelnikov and E.A. Vasiliev, *Int.J.Mod.Phys. A* 20, 4217 (2005)
- [14] F. Munyaneza and P.L. Biermann, *astro-ph/0403511*
- [15] J.D. MacMillan and R.N. Henriksen, *ApJ* 569, 83 (2002)
- [16] F.C. Michel, *Astr.Sp.Sci.* 15, 153 (1972)
- [17] M.C. Begelman, *A&A* 70, 583 (1978)
- [18] W. Brinkmann, *A&A* 85, 146 (1980)
- [19] T.K. Das and A. Sarkar, *A&A* 374, 1150 (2001)
- [20] I. Mandal, A.K. Ray and T.K. Das, *astro-ph/0702733*
- [21] K.S. Thorne, R.A. Flammang and A.N. Zytlow, *MNRAS* 194, 475 (1981)
- [22] R.A. Flammang, *MNRAS* 199, 833 (1982)
- [23] L. Nobili, R. Turolla and L. Zampieri, *ApJ* 383, 250 (1991)
- [24] M.-G. Park, *MNRAS* 367, 1739 (2006)
- [25] S.K. Chakrabarti, *Phys.Rep.* 266, 229 (1996)
- [26] J.D. MacMillan and R.N. Henriksen, in *Coevolution of Black Holes and Galaxies*, ed. L.C. Ho, *Carnegie Observatories Astrophysical Series*, vol. I, 2004
- [27] D. Lynden-Bell, *MNRAS* 136, 101 (1967)
- [28] S. Tremaine, M. Hénon and D. Lynden-Bell, *MNRAS* 219, 285 (1986)
- [29] J.E. Taylor and J.F. Navarro, *ApJ* 563, 483 (2001)
- [30] E. Rasia, G. Tormen and L. Moscardini, *MNRAS* 351, 237 (2003)
- [31] R.N. Henriksen, *ApJ* 653, 894 (2006)
- [32] R.N. Henriksen, *ApJ* 671, 1147, (2007)
- [33] S. Peirani, F. Durier and J.A. de Freitas Pacheco, *MNRAS* 367, 1011 (2006)
- [34] S. Peirani and J.A. de Freitas Pacheco - *astro-ph/0701292*
- [35] Ya.B. Zeldovich and I.D. Novikov in *Relativistic Astrophysics*, vol. 1, The University of Chicago Press, Chicago, 1972.
- [36] H.M.P. Couchman, P.A. Thomas and F.R. Pearce, *ApJ* 452, 797 (1995)
- [37] M. Davis, G. Efstathiou, C.S. Frenk and S.D.M. White, *ApJ* 292, 371 (1985)
- [38] S. Peirani, R. Mohayaee and J.A. de Freitas Pacheco, *MNRAS* 348, 921 (2004)
- [39] K. Gebhardt et al. *ApJ* 539, 13 (2000)
- [40] S. Tremaine et al., *ApJ* 574, 740 (2002)
- [41] Onken, C. A., Ferrarese, L., Merritt, D., Peterson, B. M., Pogge, R. W., Vestergaard, M., & Wandel, A. 2004, *Apj*, 615, 645
- [42] Baes, M., Buyle, P., Hau, G. K. T., & Dejonghe, H. 2003, *MNRAS*, 341, L44
- [43] L. Miller, W.J. Percival, S.M. Croom and A. Babic, *A&A* 459, 43 (2006)
- [44] P. Young, *ApJ* 242, 1232 (1980)